

Seat No. **OCT-NOV 2025 WINTER EXAMINATION****1154 B.Tech. CBCS****Sub. Name: Engineering Maths - III****Sub. Code: 63338/73197/77769****Day and Date: Tuesday ,16-12-2025****Total Marks: 70****Time: 02:30 PM To 05:00 PM****Instructions:**

- Special Inst.:**
1. Attempt any three full questions from each section.
 2. Figures to the right indicate full marks.
 3. Use of non- programmable scientific calculator is allowed.

Q1) Solve the following. [12]

a) Solve $\frac{d^3y}{dx^3} - 3\frac{d^2y}{dx^2} + 4y = e^{2x}$ [6]

b) Solve $(D^2 + D + 1)y = \sin 2x$ [6]

Q2) Solve the following. [11]

a) Find the angle between the surfaces, $x^2 + y^2 + z^2 = 9$ and $z = x^2 + y^2 - 3$ at the point $(2, -1, 2)$ [5]

b) Find the directional derivative of $\phi = 2x^3y - 3y^2z$ at $P(1, 2, -1)$ in the direction of $Q(3, -1, 5)$. In what direction from P is the directional derivative maximum? [6]

Q3) Solve the following. [11]

- a) Obtain the equation of line of regression of cost on age from the following table giving the age of car of certain make and the annual maintenance cost. [5]

Age of car(x)	2	4	6	8
Maintenance(y)	1	2	2.5	3

- b) Fit a straight line to the following data: [6]

x	1	2	3	4	6	8
y	2.4	3	3.4	4	5	6

Q4)

Attempt any two from the following.

- a) The deflection of a strut of length l with one end ($x=0$) built in and the other supported and subjected to end thrust P , satisfies the differential equation

$$\frac{d^2y}{dx^2} + a^2y = \frac{a^2R(1-x)}{P}, \text{ where } a^2 = \frac{P}{EI}$$

Find the equation of the deflection curve. Given that $\frac{dy}{dx} = y = 0$ when $x=0$. [6]

- b) Find the directional derivative of the function $F(x, y, z) = x^2 + xy + z^2$ at the point $A(1, -1, -1)$ in the direction of the line AB where B has co-ordinates $(3, 2, 0)$. [6]

- c) Using the method of least squares fit a curve of the form $y=ab^x$ to the following data.

x	1	2	3	4
y	4	11	35	100

[6]

Q5)

SECTION-II

[12]

Solve the following.

- a) If the mean and variance of a Binomial distribution are 4 & 2 respectively, find the probability of [6]

(i) Exactly 2 successes (ii) less than 2 successes (iii) atleast 2 successes

- b) A company produces condensers and supply them in the packs of 5 condensers each. If 1.5% of the condensers produced by the company are defective, using Binomial probability distribution find: [6]

- (i) Probability that a pack selected at random from the production line is free from defective condensers.
 (ii) A pack selected at random from the production line contain atleast one defective condenser.

Q6)

Solve the following.

[11]

- a) Find the laplace transform of $\frac{e^{-3t} \sin 4t}{t}$ [5]

- b) Evaluate using laplace transform $\int_0^{\infty} e^{-3t} t \cdot \sin t dt$ [6]

Q7)

Solve the following.

[11]

- a) Evaluate $\int_{-3}^3 x^4 dx$ by using Trapezoidal rule taking 6 equal sub intervals. [5]

- b) Evaluate $\int_4^{5.2} \log_e x dx$ using Simpson's $\left(\frac{3}{8}\right)^{th}$ rule by dividing the interval

$[4, 5.2]$ into 6 equal parts. [6]

Q8)

[2]

P.T.O.

Attempt any two of the following.

- a) Marks obtained by a student are normally distributed with mean 55 and standard Deviation 5. If 1000 students appear in an examination [6]
- (i) how many students will get marks more than 40?
- (ii) how many students will get marks in between 45 to 50?
- [Given: Area under normal curve from $z = 0$ to $z = 3$ is 0.4987, area under normal curve from $z = 0$ to $z = 2$ is 0.4773, area under normal curve from $z = 0$ to $z = 1$ is 0.3413]
- b) Find inverse laplace transform of $\frac{2s+3}{(s+1)^2(s+2)}$ [6]
- c) Evaluate $\int_0^1 \frac{dx}{1+x^2}$ using Weddle's rule by dividing the interval into 6 equal sub intervals. [6]

End Of Question Paper

Important Note for Chief Exam Officer / SRPD Coordinator / Sr Supervisor/ Student -

This Question Paper may be distributed for following Subjects as common code.

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- 1] (101) Bachelor of Engineering (77769) Engineering Maths - III Part 2 SEM 3
- 2] (1154) B.Tech. CBCS (73197) Engineering Maths - III Part 2 SEM 3
- 3] (101) Bachelor of Engineering (63338) Engineering Maths-III Part 2 SEM 3