

Seat No. **OCT-NOV 2025 WINTER EXAMINATION**

1154 B.Tech. CBCS

Sub. Name: Engineering Mathematics-III

Sub. Code: 63350/73203/77734

Day and Date: Tuesday ,16-12-2025

Total Marks: 70

Time: 02:30 PM To 05:00 PM

**Instructions:**

- Special Inst.:**
- 1) Attempt any Three questions from Q. no. 1 to 4.
  - 2) Attempt any Three questions from Q. no. 5 to 8.
  - 3) Figures to the right indicate full marks.
  - 4) Use of non-programmable calculator is allowed.
  - 5) Assume suitable data if necessary.

Q1) Solve [12]a. Solve  $(D^2 + 3D + 2)y = \sin 2x$  [6]b. Solve  $(D^3 - 7D - 6)y = (1 + x^2) e^{2x}$  [6]Q2) Solve [11]a. Fit a straight line  $y = a + bx$  for the following data. [5]

|   |    |    |    |    |    |    |
|---|----|----|----|----|----|----|
| x | 0  | 5  | 10 | 15 | 20 | 25 |
| y | 12 | 15 | 17 | 22 | 24 | 30 |

b. Find the equation of line of regression y on x for the following data. [6]

|   |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|
| x | 40 | 34 | 28 | 30 | 44 | 38 | 31 |
| y | 32 | 39 | 26 | 30 | 38 | 34 | 28 |

Q3) Solve [11]a. Evaluate using Laplace transform  $\int_0^{\infty} e^{-2t} t \cos t dt$ . [5]b. Find the inverse Laplace transform of  $\frac{5s^2 + 8s - 1}{(s+3)(s^2+1)}$  [6]Q4) Attempt any Two of the following [12]

a. Solve  $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 4y = 2x$  [6]

b. Fit the curve  $y = ab^x$  to the following data. [6]

|   |   |     |     |     |     |     |     |     |
|---|---|-----|-----|-----|-----|-----|-----|-----|
| x | 1 | 2   | 3   | 4   | 5   | 6   | 7   | 8   |
| y | 1 | 1.2 | 1.8 | 2.5 | 3.6 | 4.7 | 6.6 | 9.1 |

c. Using Laplace transform solve  $(D^2 + 4D + 8)y = 1$  with  $y(0) = 0$  and  $y'(0) = 1$ . [6]

Q5) Solve [11]

a. Show that the vector field [6]

$\vec{F} = (y \sin z - \sin x) i + (x \sin z + 2yz) j + (xy \cos z + y^2) k$  is irrotational and find its scalar potential.

b. Find the directional derivative of  $\phi = x^2yz + 4xz^2$  at  $(1, -2, 1)$  in the direction of  $2i - j - 2k$ . [5]

Q6) Solve [12]

a. Obtain the Fourier series expansion for  $f(x) = 4 - x^2$  in  $(0, 2)$ . [7]

b. Find the Fourier series for  $f(x) = x$  in the interval  $(-\pi, \pi)$ . [5]

Q7) Attempt any one from the following. [11]

a.

Solve the Laplace equation  $u_{xx} + u_{yy} = 0$  for following square mesh with boundary values as shown in the figure by Gauss-Seidel method. Carry out two iterations.

|   |   |       |       |       |      |      |
|---|---|-------|-------|-------|------|------|
|   | 0 | 8.7   | 12.1  | 12.8  | 9.0  |      |
| 0 |   |       |       |       |      | 17.0 |
|   |   | $u_7$ | $u_8$ | $u_9$ |      |      |
| 0 |   |       |       |       |      | 21.0 |
|   |   | $u_4$ | $u_5$ | $u_6$ |      |      |
| 0 |   |       |       |       |      | 21.9 |
|   |   | $u_1$ | $u_2$ | $u_3$ |      |      |
|   | 0 | 11.1  | 17.0  | 19.7  | 18.6 |      |

- b. Determine the solution of one-dimensional heat equation  $\frac{\partial u}{\partial t} = c^2 \frac{\partial^2 u}{\partial x^2}$  under the boundary conditions  $u(0, t) = 0$ ,  $u(l, t) = 0$  and  $u(x, 0) = x$ ,  $0 < x < l$  where  $l$  being the length of the rod. [11]

Q8) Attempt any Two from the following. [12]

- a. Obtain the Fourier series expansion for  $f(x) = \begin{cases} 1 + \frac{2x}{\pi}, & -\pi \leq x \leq 0 \\ 1 - \frac{2x}{\pi}, & 0 \leq x \leq \pi \end{cases}$  [6]

- b. Find the angle between the normals to the surfaces  $x^2y + z = 3$  and  $x \log z - y^2 + 4 = 0$  at the point  $(-1, 2, 1)$ . [6]

- c. Using the method of separation of variables, Solve [6]

$$\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} = 0$$

## End Of Question Paper

**Important Note for Chief Exam Officer / SRPD Coordinator / Sr Supervisor/ Student -**

This Question Paper may be distributed for following Subjects as common code.

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