

F.Y.B.Tech.(All Branches) (Part-I) (Semester-II) (CBCS)
Examination, Oct.-2025
ENGINEERING MATHEMATICS-II
Sub. Code: 72500

Day and Date : Friday, 16-01-2026
Time : 10.30 a.m. to 1.00 p.m.

Total Marks : 70

Instructions :

- 1) Attempt any three questions from each section.
- 2) Figures to the right indicate full marks.
- 3) Use of non-programmable calculator is allowed.

SECTION-I

- Q. 1) a) Solve $(\sec x \tan x \tan y + 4x^3)dx + (\sec x \sec^2 y + \cos y)dy = 0$. [6]
- b) Solve $(x^4 e^x - 2mxy^2)dx + 2mx^2 y dy = 0$. [6]
- Q. 2) a) Find the orthogonal trajectory of $\frac{x^2}{a^2} + \frac{y^2}{b^2 + \lambda} = 1$ where λ is parameter. [5]
- b) In a circuit containing resistance R, inductance L and a constant e. m. f. E, the current i is given by $L \frac{di}{dt} + Ri = E$. If $L = 640$ h, $R = 250 \Omega$, $E = 500$ V and $i = 0$ when $t = 0$, show that the current will approach 2 amp, when $t \rightarrow \infty$. [6]
- Q. 3) a) Use Taylor's series method to solve $\frac{dy}{dx} = 1 + xy$, with $y(1) = 2$ at $x = 1.2$. [6]
- b) Use Euler's modified method to solve $\frac{dy}{dx} = x^2 + y$, with $y(0) = 1$ at $x = 0.1$ taking $h = 0.05$. [5]
- Q. 4) Attempt any TWO of the following.
- a) Solve $3y^2 \frac{dy}{dx} + 2xy^3 = 4x^3 e^{x^2}$. [6]
- b) A body at temperature $80^\circ C$ is placed in a room temperature at $50^\circ C$ at time $t = 0$. At the end of 5 minutes the body has cooled to temperature $70^\circ C$. Find the temperature of the body after 10 minutes. [6]
- c) Apply Runge-Kutta's method of fourth order to solve $\frac{dy}{dx} = x + y^2$, with $y(0) = 1$ at $x = 0.1$. [6]

SECTION-II

- Q.5) a) Perform five iterations of the bisection method to obtain the positive root of the equation $\sin x = \frac{1}{x}$ that lies between $x = 1$ and $x = 1.5$. [6]
- b) Find the positive root of the equation $x^4 - x - 10 = 0$ correct to three decimal places using Secant method. [6]
- Q.6) a) Evaluate $\int_0^{\infty} 5^{-4x^2} dx$. [5]
- b) Evaluate $\int_0^2 x^4 (8 - x^3)^{-\frac{1}{3}} dx$. [6]
- Q.7) a) Evaluate $\int_0^a \int_0^{\sqrt{a^2-x^2}} \sqrt{a^2 - x^2 - y^2} dy dx$. [5]
- b) Evaluate by Changing to polar coordinates $\int_0^{4a} \int_{\frac{y}{4a}}^y dx dy$. [6]
- Q.8) Attempt any TWO of the following.
- a) Using Newton-Raphson method, find the real root of $x \log_{10} x = 1.2$ correct to five decimal places. [6]
- b) Express $\operatorname{erf}(x)$ as an infinite series and find $\operatorname{erf}(0.5)$. [6]
- c) Find the area between $y^2 = 4x$ and the chord AB joining the points A (1,2) and B (1,-2). [6]

